By writing my name above, I affirm that this test represents my work only, without aid from outside sources. In all aspects of this course I perform with honor and integrity.

Show your work on all of the problems. Your approach to the problem is as important as, if not more IMPORTANT THAN, YOUR ANSWER. DRAW CLEAR AND NEAT PICTURES SHOWING COORDINATE SYSTEMS AND ALL OF THE RELEVANT PROBLEM VARIABLES. ALSO, EXPLICITLY SHOW THE BASIC EQUATIONS YOU ARE USING. BE NEAT AND THOROUGH. THE EASIER IT IS FOR ME TO UNDERSTAND WHAT YOU ARE DOING, THE BETTER YOUR GRADE WILL BE.

1) Starting with the unit vector expression for the position, r, of a particle constrained to move in a circle, derive an expression for the magnitude of the velocity vector and the magnitude of the acceleration vector assuming that the particle is moving in uniform circular motion.

Include a picture with the position vector, r, the velocity vector, v, the acceleration vector, a, and the position angle,  $\theta$ , clearly marked. assume: I and do are const.

Clearly state any assumptions required by the proof.

$$\vec{r} = r_{x} x + r_{y} \hat{j}$$

$$\vec{r} = r \cos\theta x + r \sin\theta \hat{j}$$

$$\vec{v} = \frac{d\vec{r}}{dt} = r \frac{d}{dt} \left( \cos\theta x + \sin\theta \hat{j} \right)$$

$$= r \left( -\frac{d\theta}{dt} \sin\theta x + \frac{d\theta}{dt} \cos\theta \hat{j} \right)$$

$$\vec{v} = r \frac{d\theta}{dt} \left( \sin\theta x + \cos\theta \hat{j} \right)$$

$$\vec{v} = r \omega \int_{0}^{\infty} \omega = \frac{d\theta}{dt}$$

$$\vec{a} = \frac{d\vec{v}}{dt} = r\omega \frac{d}{dt} \left( -SINOL + COSOJ \right)$$

$$= r\omega \frac{d\theta}{dt} \left( -COSOL - SINOJ \right)$$

$$a = r\omega^2$$

### SAMPLE TEST 2 Phys 111 Fall 2010

2) Multiple Choice, 4 points each.

2.1) If you jumped out of a plane, you would begin speeding up as you fell downward. Eventually, due to wind resistance, you will fall at a constant velocity. At this point, the force due to wind resistance is

-1	alialette.	ama a 11 am	than	tha.	faraa	of	amor zity z
a)	slightly	smaner	man	une	TOTCE	OI	gravity

constant V, Net Force

must be zero.

d) greater than the force of gravity

2.2) You are making a circular turn in your car when you hit a big patch of ice causing the frictional force between the tires and the road to go to zero. While the car is on the ice, it

a) moves in a straight line

No net Force in

b) continues on a circular path but with a larger radius

horizontal directions.

c) follows the original circular path

d) follows a curved path that is non-circular

2.3) A merry-go-round is spinning with a fixed angular speed. As you walk from the center towards the edge

a) the force provided by static friction must increase so that you don't slide off.

b) the force provided by static friction must decrease so that you don't slide off.

c) The force provided by static friction remains constant and you don't slide off.

2.4) A rock tied to a string is being whirled in a circle. In the absence of gravity, the tension in the string is

A) 
$$F_T = mg$$

$$F_T = m \frac{v}{r}$$

A) 
$$F_T = mg$$
  
B)  $F_T = m\frac{v}{r}$   
C)  $F_T = mr\omega^2$   
D)  $F_T = r\omega^2$ 

$$(C)$$
  $F_T = mr \omega^2$ 

2.5) Consider a person standing in an elevator that is accelerating downward. The magnitude of the upward normal force exerted by the elevator floor on the person is

a) larger than

b) less than

c) equal to

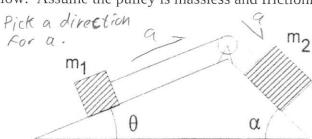
the magnitude of the weight of the person.

al mg weight"

## SAMPLE TEST 2 PHYS 111 FALL 2010

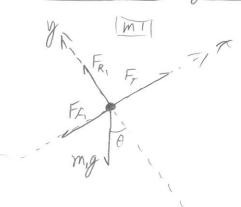
**3**) Consider the figure shown below. Assume the pulley is massless and frictionless.

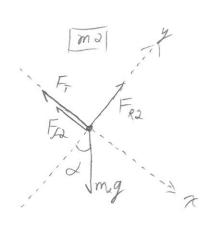
$$\theta = 30^{\circ}$$
  
 $\alpha = 45^{\circ}$   
 $\mu_k = 0.10$   
 $m_1 = 5.0 \text{ kg}$   
 $m_2 = 15.0 \text{ kg}$ 



- a) Find an expression (no numbers) for the acceleration of the system.
- b) Plug in the numbers and find the numeric answer.

# Free Body Diagrams





OF-F,-M,gSINO=M,a

②  $F_{RI} - m_i g \cos \theta = 0$ 

$$\sum F_{x} = Md_{x}$$

 $m_{s}gsind-F_{7}-F_{F_{2}}=m_{s}a$  (4)  $F_{R2}-m_{s}gcosd=0$ 

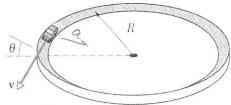
continued

```
Sample Test 2 - P3 continued
* Rewrite Friction terms using: Fr = UKFR
From O: Fr - Mx FRI - Mig SINO = Mi, Q (5)
 From 3: mg SINX - F, - Mx FR2 = M2 a 6
* solve @ and @ For Fx and subst, into 6 and 6
 Subst @ 76;
         FT - UKM, gCOSO - M, gSINO = M, d
  Subst 4 76:
         m, g SINX - F, - M, m, g cosx = m, a
* Solve @ For Fr and subst into 8
       mag SINZ -UKM, gCOSO - M, gSINO - M, a-UKM, gCOSZ = MA
    = g \left[ m_2 \left( SIN d - M_R COS d \right) - m_1 \left( SIN \theta + M_R COS \theta \right) \right] = Q \left( m_1 + m_2 \right)
   Q = g \frac{m_2(SINd - M_KCOSd) - m_1(SIND + M_KCOSO)}{(m_1 + m_2)}
 b)
    a = 9.8 - \frac{(15)(51N(45) - (0.10)(05(45)) - (5.0)(51N(30) + (0.10)(05(20))}{}
                                  50+15-0
```

 $a = 3.24 \text{ m/s}^2$ 

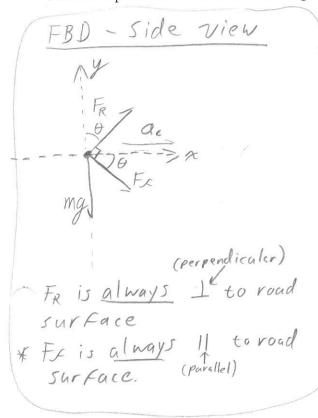
### Sample Test 2 Phys 111 Fall 2010

4) Curves on roadways are often banked so that the reaction force from the road provides part of the centripetal acceleration required to keep the car moving around the circle.



Assume the road is a circle of radius R, the car is going some velocity v, and the tires have some coefficient of static friction  $\mu_s$ .

Find an expression for the minimum angle required to keep the car on the road in terms of R, v, and  $\mu_s$ .



NSL

$$\chi: \Sigma F_{2} = Ma_{\chi}$$
 centripetal

 $F_{R}SIN\theta + F_{R}COS\theta = Ma_{\chi}$ 
 $\Rightarrow F_{R}SIN\theta + M_{S}F_{R}COS\theta = M_{R}^{2}$ 
 $\Rightarrow F_{R}SIN\theta + M_{S}F_{R}COS\theta - M_{R}^{2}$ 
 $\Rightarrow F_{R}COS\theta - F_{R}SIN\theta - M_{R}^{2} = O$ 
 $\Rightarrow F_{R}COS\theta - M_{S}F_{R}SIN\theta - M_{R}^{2} = O$ 
 $\Rightarrow F_{R}COS\theta - M_{S}F_{R}SIN\theta - M_{R}^{2} = O$ 

From 
$$O: F_R(S \pm N\theta + M_s COS\theta) = M \frac{v^2}{R}$$
  
From  $O: F_R(S \pm N\theta + M_s COS\theta) = Mg$   
Divide  $\frac{1}{2}: \frac{F_R(S \pm N\theta + M_s COS\theta)}{F_R(COS\theta - M_s SIN\theta)} = \frac{M \frac{v^2}{R}}{Mg}$ 

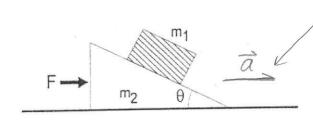
Given
R, V, Us
Want

 $= 2RSIN\theta + M_s gR(OS\theta = V^2COS\theta - M_s V^2SIN\theta)$   $= (gR + M_s V^2)SIN\theta = (V^2 - M_s gR)cos\theta$   $= 2RSIN\theta = \frac{V^2 - M_s gR}{gR + M_s V^2}$ 

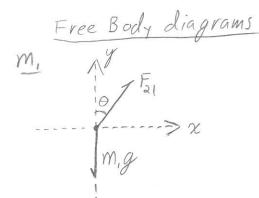
#### Sample Test 2 Phys 111 Fall 2010

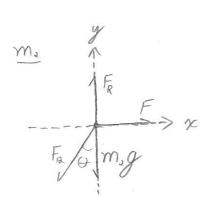
In the figure shown below all surfaces are frictionless. Find an expression for the the force applied to block  $m_2$  so that block  $m_1$  does not slide down the ramp.





Both blocks are accelerating parallel to the Floor. with the same accel.





NSL

m,

 $x: \Sigma F_x = Ma_x$ 

O FISINO = Ma

 $y: \Sigma F_y = Ma_y$ 

(1) F, coso - m, g = 0

m

x: Zfa = Max

3) F-FISIND = Maa

(9 y: FR - FD(OSA - M.g = 0

\* To solve @ For E, I'll eliminate a with eq O and eliminate E, with eq. (2).

Continued

Divide 
$$\frac{G}{D}$$
:  $\frac{F-F_0SINO}{F_0SINO} = \frac{m_0 \alpha}{m_0 \alpha} \implies F-F_0SINO = \frac{m_0}{m_0} F_0SINO$ 

$$= F = F_1, SINO(1 + \frac{M_2}{m_1})$$

From (a): 
$$F_{i,i} = \frac{m_{i,j}g}{\cos g}$$

$$F = \frac{m_i g}{\cos \theta} SINO \left(1 + \frac{m_i}{m_i}\right)$$

=> 
$$F = M_1 \left(1 + \frac{M_2}{m_1}\right) g + an\theta$$

=) 
$$F = \left( m_1 + m_2 \frac{m_3}{m_1} \right) g \tan \theta$$

$$= |F = (m_1 + m_2) g \tan \theta$$