

## Rotation – Set 5

1

Two meter sticks are stood in the corner where the floor meets the wall. One has a large mass attached to the end furthest from the corner. Which one hits the ground first?

We'll solve the problem by calculating the *Angular Acceleration* of each object and then comparing them.

a) Calculate the angular acceleration of the meter stick falling over under the influence of gravity.

b) Calculate the angular acceleration of a meter stick with a large mass attached to its end falling over under the influence of gravity.

c) Take the ratio  $\frac{\alpha_a}{\alpha_b}$ . Is it greater than or less than one? Which stick hits the ground first?

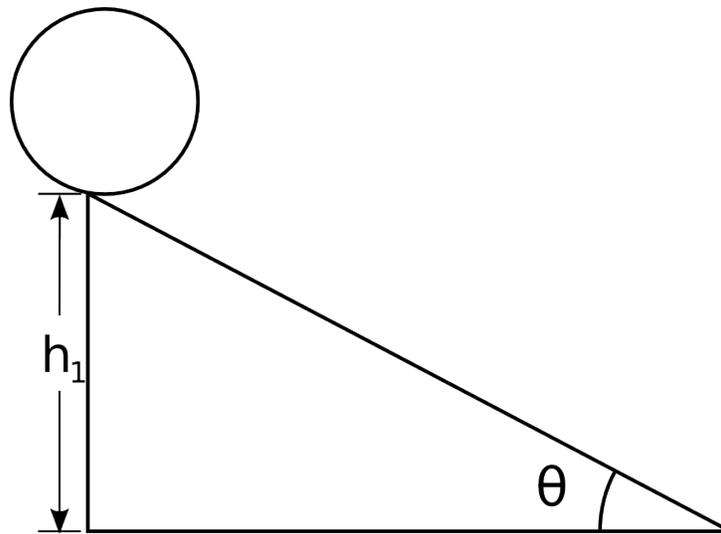
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3

Use **Torque and Kinematics** to solve this problem.

A rolling object with a radius  $R$ , mass  $m$ , and moment of inertia  $I$ , starts from rest at the top of an incline plane of height  $h$  that makes an angle  $\theta$  with the horizontal.

- Find an expression for the linear and angular acceleration,  $\alpha$ , of the object in terms of  $I$ ,  $m$ ,  $R$ ,  $g$ , and  $\theta$ .
- Using kinematics, find an expression for the linear and angular velocity of the object at the bottom of the ramp in terms of  $I$ .
- Assume that the object is a disk with  $I = \frac{1}{2}mR^2$  and plug  $I$  into your velocity expressions. Verify that your answers are the same as when you solved this problem using energy.



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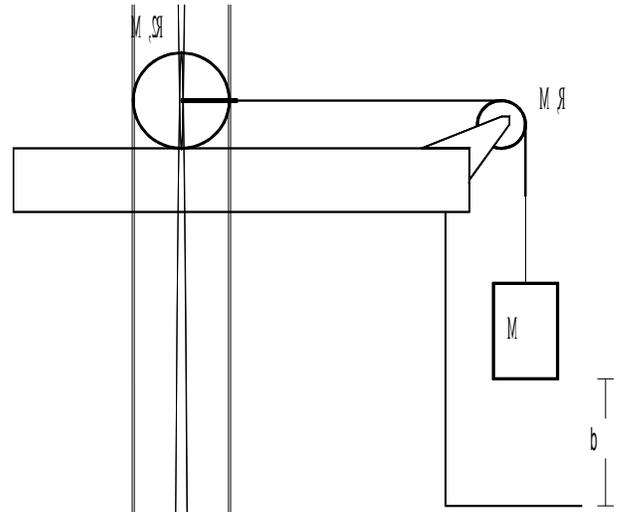
4

Use **Torque and Newton's Second Law** solve this problem.

A solid cylinder (radius =  $2R$ , mass =  $M$ ) rolls without slipping as it is pulled by a massless yoke attached to a string. The string goes over a frictionless pulley shaped as a solid disk (radius =  $R$ , mass =  $M$ ) and is attached to a hanging weight (mass =  $M$ ).

$$I_{cylinder} = \frac{1}{2} MR^2$$

What is the acceleration of the system?



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5

Use **Torque and Newton's Second Law** solve this problem.

A block of mass  $M$  rests on a rough table with  $\mu_k = 0.3$ . A massless string is attached to the block, wrapped around a solid cylinder having a mass  $M$  and a radius  $R$ , runs over a massless frictionless pulley, and is attached to a second block of mass  $M$  that is hanging freely.

Find the acceleration of this system.

$$I_{cylinder} = \frac{1}{2} MR^2$$

