

Name: _____

By writing my name above, I affirm that this test represents my work only, without aid from outside sources. In all aspects of this course I perform with honor and integrity.

SHOW YOUR WORK ON ALL OF THE PROBLEMS. YOUR APPROACH TO THE PROBLEM IS AS IMPORTANT AS, IF NOT MORE IMPORTANT THAN, YOUR ANSWER. DRAW **CLEAR AND NEAT PICTURES** SHOWING COORDINATE SYSTEMS AND ALL OF THE RELEVANT PROBLEM VARIABLES. ALSO, **EXPLICITLY** SHOW THE **BASIC EQUATIONS** YOU ARE USING. BE NEAT AND THOROUGH. THE EASIER IT IS FOR ME TO UNDERSTAND WHAT YOU ARE DOING, THE BETTER YOUR GRADE WILL BE.

A few potentially useful equations

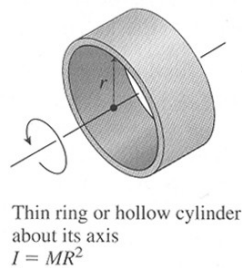
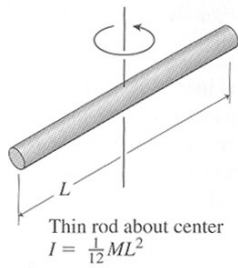
Moment of Inertia, discrete definition

Moment of Inertia, integral definition

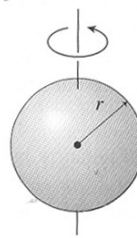
Parallel Axis Theorem

Superposition

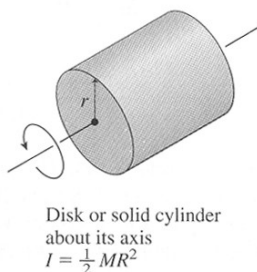
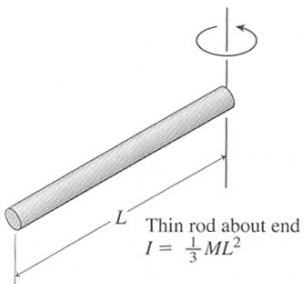
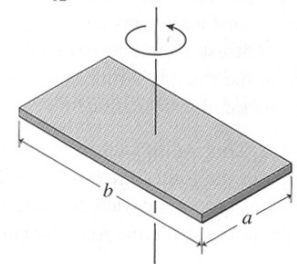
TABLE 10.2 Rotational Inertias



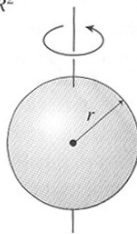
Solid sphere about diameter
 $I = \frac{2}{5}MR^2$



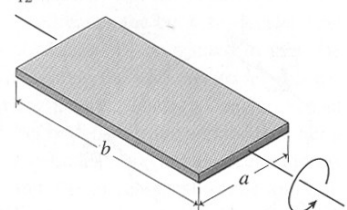
Flat plate about perpendicular axis
 $I = \frac{1}{12}M(a^2 + b^2)$



Hollow spherical shell about diameter
 $I = \frac{2}{3}MR^2$



Flat plate about central axis
 $I = \frac{1}{12}Ma^2$



SAMPLE TEST 6
PHYS 111, FALL 2011, SECTION 1

1) Derivations

a) (10pts) Given a differential equation of the form $m\ddot{x} + b\dot{x} + kx = F_0 \cos(\omega t)$, write the general solution for $x(t)$, $\dot{x}(t)$, and $\ddot{x}(t)$ in terms of the angular frequency ω , the amplitude A , and the phase angle ϕ .

b) (10pts) Given the boundary conditions $x(0) = x_0$ and $\dot{x}(0) = v_0$, derive an expression for the phase angle ϕ and the amplitude A in terms of x_0 , v_0 , and ω .

SAMPLE TEST 6
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2) Multiple Choice

- 2.1) A mass attached to a spring oscillates with a period T . If the amplitude of the oscillation is doubled, the period will be:
- A) T
 - B) $1.5 T$
 - C) $2T$
 - D) $\frac{1}{2} T$
 - E) $4T$
- 2.2) An object of mass m , oscillating on the end of a spring with spring constant k has amplitude A . Its maximum speed is:
- A)
 - B)
 - C)
 - D)
- 2.3) In simple harmonic motion, the magnitude of the acceleration is greatest when:
- A) the displacement is zero
 - B) the displacement is maximum
 - C) the speed is maximum
 - D) the force is zero
 - E) the speed is between zero and its maximum

SAMPLE TEST 6
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2.4) The displacement of an object oscillating on a spring is given by
If the initial displacement is zero and the initial velocity is in the negative x direction, then the phase constant ϕ is:

- A) 0 radians
- B) $\pi/2$ radians
- C) π radians
- D) $3\pi/2$ radians
- E) 2π radians

2.5) A simple pendulum of length L and mass M has frequency f. To increase its frequency to 2f:

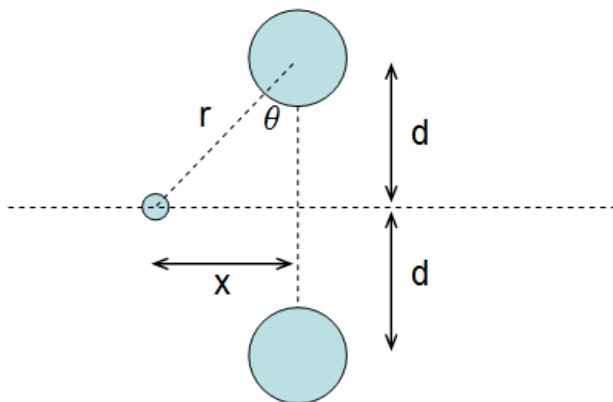
- A) increase its length to 4L
- B) increase its length to 2L
- C) decrease its length to L/2
- D) decrease its length to L/4
- E) decrease its mass to $< M/4$

SAMPLE TEST 6

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Two identical objects of mass \mathbf{M} are held rigidly in space and separated by a distance of $2\mathbf{d}$. A small mass is released from rest as shown below. The masses interact via gravity. The small mass oscillates back and forth with a period of τ .

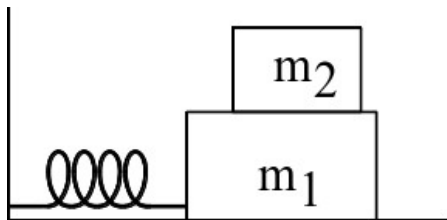
Assume that \mathbf{x} is much smaller than \mathbf{d} and find the mass \mathbf{M} in terms of π , \mathbf{d} , \mathbf{G} and τ .



SAMPLE TEST 6

PHYS 111, FALL 2011, SECTION 1

A large block m_1 executes simple harmonic motion as it slides across a frictionless surface with a frequency of $f = 1.50$ Hz. Block m_2 rests on m_1 , as shown in the figure below. The coefficient of static friction between the two blocks is $\mu_s = 0.600$. What maximum amplitude of oscillation can the system have if block m_2 is not to slip?



SAMPLE TEST 6
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In the system shown below each of the three springs have a spring constant of 50 N/m and the bar is mounted on a frictionless pivot at its midpoint. The period of small oscillations is found to be 2.0 s.

The moment of inertia for the beam is _____ .

What is the mass of the bar?

