An aging hippie is jammin' to his old "In-A-Gadda-Da-Vida" album. The turntable on which the record sits spins it with a constant angular speed of 33.33 revolutions per minute. The hippie notices that when he turns off the turntable motor, the record makes exactly three revolutions before stopping.

- a) What's the angular deceleration of the record in radians per second, man? (Assume it's a constant.)
- b) He also notices that when he starts the turntable, it takes the record 3.0 seconds to come up to speed. After the record gets up to speed, "In-A-Gadda-Da-Vida" plays for an agonizing 3.50 minutes. What is the total angular displacement of the record at the end of the song?



a)



$$\theta_0 = 0$$

$$Q = 3 \text{ rev}$$

$$Q = 33.3 \text{ rev}_{mix} = 33.3 \text{ rev}_{mix} \cdot \frac{1}{60} \frac{\text{min}}{5} = 0.55 \text{ rev}_{5}$$

$$Q = 0$$

$$\theta = \theta_0 + \omega_0 t + \beta_0 t^2$$

$$\theta = \omega_0 t + \beta_0 t^2$$

$$\omega = \omega_0 + zt$$

$$0 = \omega_0 + \alpha t$$

$$= t = -\frac{\omega_0}{t}$$

$$\theta = -\frac{\omega_0^2}{\omega} + \frac{1}{2} \times \frac{\omega_0^2}{\omega^2}$$

$$\theta = -\frac{1}{2}\frac{\omega_o^2}{2} = \frac{1}{2}\frac{\omega_o^2}{\theta}$$

$$\angle = -\frac{1}{2} \frac{33.3^2}{3} = -184 \text{ reymin}^2$$

or
$$\mathcal{L} = -\frac{1}{2} \frac{(0.55)^2}{3} = 0.05 \text{ rev/s}^2 = 0.314 \text{ rad/s}^2$$

During acceleration

$$\theta_i = 3 \propto t_i^2$$

$$\Rightarrow \theta_1 = \lambda \frac{\omega}{x} t_1^x$$

t,=3,Q. = 0.05m

$$\Rightarrow x = \frac{\omega}{t}$$

$$\theta_{3} = \theta_{1} + \omega_{1} t_{2}$$

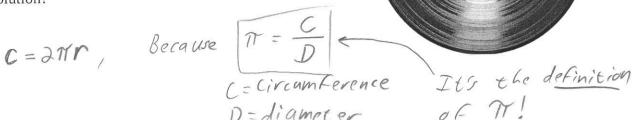
$$= \partial_s = \omega_i (t_2 + t_3)$$

$$\Theta_{s} = 33.3 \frac{\text{rev}_{min}}{3} \left(\frac{1}{3} (0.05 \, \text{m}) + 3.5 \, \text{m} \right)$$

$$\theta_s = 117 \text{ revolutions}$$

Your hippie friend is fascinated by watching a quarter on his record go around and around and around. He's somehow managed to formulate a few questions about the quarter that he needs your help answering.

a) So dude, like, if I totally put the quarter a distance r from the center, like, what distance, c, does it go in one revolution?



b) Groovy, so then, like, how far does the quarter go, let's call the distance s, if the record rotates

through an angle
$$\theta$$
.

I like to use a ratio. θ in degrees

 θ in radians

 θ = $\frac{S}{\theta} = \frac{S}{2\pi r}$
 θ = $\frac{S}{360} = \frac{S}{2\pi r}$
 $S = \frac{S}{360} = \frac{S}{3\pi r}$

OF TY!

c) Woah! Trippy... so then how FAST, is the quarter moving, call it v, in terms of the angular velocity ω?

velocity
$$\omega$$
?

If: $s = r\theta$ and $\omega = \frac{d\theta}{dt}$, then let's take the derivative
$$\frac{ds}{dt} = r\frac{d\theta}{dt} \implies V = r\omega$$

d) Right on! So like, let's say the record totally has angular acceleration, α ! What's the *tangential* acceleration, a_T, of the quarter?

Again,
$$V=r\omega$$
 and $\mathcal{L}=\frac{d\omega}{dt}$
So: $\frac{dV}{dt}=r\frac{d\omega}{dt}=\sum_{\alpha_{i}} \frac{1}{|\alpha_{i}|^{2}} = r\mathcal{L}$
what's α_{i} ? oh yea! $|\alpha_{i}|=r\omega^{2}$

The hippie wants to explore rolling the record across the floor now. Thankfully, this means that the terrible music has stopped playing. Assume that the record rolls in a perfectly straight line.

- a) If the radius of the record is r = 30 cm, how far has it rolled after one revolution?
- b) What is it's total angular displacement after it has rolled 5 meters?
- c) If the initial translational velocity of the center of the record is 2 m/s, what is it's angular velocity?
- d) If the record comes to a stop after 5 m, what was is its *angular* acceleration (assuming constant acceleration).

a) It has to roll one circumference, so:
$$c = 2777 \implies c = 277(0.30m) = \boxed{1.9m}$$

b) From problem #1, we know:

$$S = r\theta$$
, with θ in radians.

$$= \partial = \frac{s}{r} = \partial = \frac{s_m}{0.3m} =$$

() We know
$$V = r\omega = 0$$
 $\omega = \frac{V}{r} = 0$ $\omega = \frac{2.0 \text{ m/s}}{0.3 \text{ m}} = \frac{6.7 \text{ rad/s}}{6.7 \text{ rad/s}}$

continued

$$= \chi = \frac{V_0}{\alpha_T} + \frac{1}{2} \frac{V_0}{\alpha_T}$$

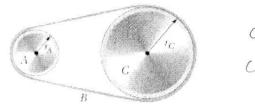
$$= 2 x = -\frac{1}{2} \frac{v_0^2}{a_i} = 2 \frac{v_0^2}{a_i} = 2 \frac{v_0^2}{a_i}$$

Then!

$$a_r = r\lambda = \frac{1}{2} \frac{v_0^2}{2} = r\lambda = \sqrt{\lambda} = \frac{v_0^2}{2rx}$$

$$\alpha = \frac{(2m)^2}{(2)(0.3n)(5m)} = 1.3 \text{ rad/}_{52}$$

A pulley of radius $r_A = 10$ cm is coupled by a belt to a pulley of radius $r_C = 25$ cm. A motor is attached to the axle of pulley A giving it an angular acceleration of $\alpha_A = 1.6$ rad/s². How long does it take pulley C to achieve an angular velocity of 100 rev/min assuming that the belt does not slip?



 $\mathcal{L}_{t} = 1.6 \operatorname{rad}_{s}^{2}$ $\mathcal{L}_{c} = 100 \frac{\operatorname{rev}}{\operatorname{min}} \cdot 20 \frac{\operatorname{rad}}{\operatorname{rev}} \cdot \frac{1}{60} \frac{\operatorname{min}}{s}^{2}$ $= 10.5 \operatorname{rad}_{s}^{2}$

We need to relate ac to a.

Because they are coupled by the belt, a point on the rim of A must have the same times acceleration as a point on the rim of C.

So,
$$\Gamma_A \mathcal{A}_A = \Gamma_C \mathcal{A}_C = \mathcal{A}_C = \frac{\Gamma_A}{\Gamma_C} \mathcal{A}_C$$

Now, using kinematics:

$$\omega = 35^{\circ} + 2t = 2 \omega_{e} = 2 t$$

$$= 2 t = 2 t = 2 t = 2 t$$

$$= 2 t = 2 t = 2 t = 2 t$$

$$= 2 t = 2 t = 2 t$$

$$= 2 t$$

A car's odometer works by counting the revolutions of the axle. A car's speedometer works by measuring the angular velocity of the axle. For the odometer and speedometer to work correctly, the correct tire radius has to be set at the factory.

My car came from the factory with tires with a diameter of $d_1 = 60$ cm. They wore out and I replaced them with tires with a diameter of $d_2 = 80$ cm.

- a) With the proper tires on the car: What is the angular displacement, θ , (in radians and revolutions) of the tire after 1.0 km? What is the angular velocity of the axle, ω , (in rad/sec and rev/sec) if I'm driving 100 km/hr?
- b) What are the answers to the questions in part a with the improper tires on the car?
- c) If I've added 10,000 km to the odometer since putting the new tires on, how many km have I actually driven the car? (HINT: The odometer *assumes* that the proper tires are on the car.)
- d) If the speed limit is 100 km/h, what should my speedometer read so that I don't get a speeding ticket? (HINT: The speedometer assumes that the proper tires are on the car.)

a)
$$d = 1 \text{km}$$
 $V = 100 \text{ km}$
 $V = 30 \text{ cm}$
 $V = 700 \text{ cm}$

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$$\omega = \frac{\frac{1000 \text{ km}}{3600 \text{ km}}}{4.0 \times 10^{-4} \text{kn}} = 69 \text{ rad/s} = 11 \text{ rev/s}$$

Odometer" distance:
$$d_A = \Gamma_A \Theta_A$$

Actual angular distance

gets Fed to the odometer

"Odometer" distance: do = 100

$$\Theta_{A} = \frac{dA}{\Gamma_{A}} \Longrightarrow d_{o} = \Gamma_{o} \frac{d_{A}}{\Gamma_{A}} \Longrightarrow \left[d_{A} = \frac{\Gamma_{A}}{\Gamma_{o}} d_{o} \right]$$

$$d_{A} = \frac{40cm \cdot 1 \times 10^{4} km}{30cm \cdot 1 \times 10^{4} km}$$

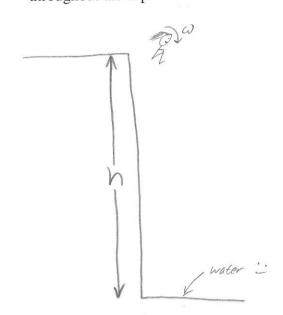
$$d_{A} = 1.3 \times 10^{4} km$$

d) Actual speed:
$$V_A = \Gamma_A \Theta_A = \Gamma_$$

Jets fed to the speedometer

$$\Theta_{A} = \frac{V_{A}}{\Gamma_{A}} \Rightarrow V_{S} = \Gamma_{S} \frac{V_{A}}{\Gamma_{A}}$$

A diver makes 2.5 complete revolutions on the way from a 10 m high platform to the water. Assume that her initial vertical velocity was zero. What was her angular velocity, assuming that it was constant throughout the trip.



$$\theta = 2.5 \text{ rev.}$$
 $\omega_0 = ?$

$$h = 10 \text{ m}$$

$$V_0 = 0$$

$$\alpha = 0$$

Rotation
$$\frac{Rotation}{\partial = \Theta_0 + W_0 t} + \frac{1}{2} \underbrace{dt^2}_{0}$$

$$\frac{\partial}{\partial t} = \frac{\partial}{\partial t} \underbrace{\partial t}_{0}$$

$$\frac{\partial}{\partial t} = \frac{\partial}{\partial t} \underbrace{\partial t}_{0}$$

$$\frac{translation}{y = y_0 + y_0$$

combine () and ()
$$\left[\omega_o = \Theta \left(\frac{g}{2h} \right)^{1/2} \right] \Rightarrow 2.5 \text{ rev} \left(\frac{g.8 \text{ m/s}^2}{2} \right)^{1/2} = \omega_o$$

$$\left[\omega_o = 1.75 \text{ rev/s} \right]$$

Rotation, moment of inertia

A wagon wheel with a radius of R=30cm with 8 equally spaced spokes is spinning with an angular velocity of ω =2.5 revolutions/sec. You want to shoot a 20 cm arrow parallel to the wheel's axle between the spokes without hitting one. Assuming that the spokes and the arrow are very thin:

a) What minimum speed must the arrow have?

b) Does it matter where between the axle and the rim you aim? If so, where is the best location?



Circle is 271 radians.

There are 8 equal wedges:

$$at: \theta = \frac{2\pi}{8} = \frac{11}{4} each$$

Let's consider that we aim the arrow a distance of above the axle. If it just misses a spoke, It has to be all the way through bofore the next spoke gets there.

The spoke is moving at V= rw
and hasto travel adistance S= ro

$$S = Ut = X\theta = K\omega t$$

$$\theta = \omega t \implies time is independent$$

$$0 \in V. continued 1$$

Jo: t= & So, the arrow travels it's longth in l=Vt=V&

> So it has to go 1 2 = 2 to 1

V = 20 cm - 25 m/s - 291 mod 8/4 rad V = 8 (25) (20) cm/s = 100 cm/s

b) Vis independent of r in part a -...
so it does not matter where you aim.