Vector Problems

A hiker begins a trip by first walking 25 km southeast from her base camp. On the second day, she walks 40 km in a direction 60° north of east.

(a) Sketch the hiker's displacement vector for day 1, \vec{D}_1 , and write the components in unit vector notation. (assume East is \hat{i} and North is \hat{j})

$$\vec{D}_{1} = D_{1} \cos \theta_{1} + D_{1} \sin \theta_{2}$$

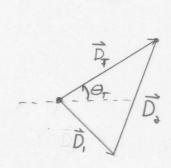
= 25 cos(-45) $\vec{\Lambda} + 25 \sin (-45) \vec{J}$
 $\vec{D}_{2} = (18\pi - 18\vec{J}) \text{ km}$

(b) Sketch the hiker's displacement vector for day 2, D_2 , and write the components in unit vector notation.

$$\vec{D}_s = D_s \cos \theta_s \hat{\lambda} + D_s \sin \theta_s \hat{J}$$

 $\vec{D}_s = 40\cos (60)\hat{\lambda} + 40\sin (60)\hat{J}$
 $\vec{D}_s = 40\cos (60)\hat{\lambda} + 36\hat{J}$

(c) Sketch the the vector sum of the total trip and solve the vector equation $\vec{D}_1 + \vec{D}_2 = \vec{D}_T$. Write \vec{D}_T in unit vector notation.



$$\vec{D}_{7} = \vec{D}_{1} + \vec{D}_{3} = 18x - 18z + 20x + 36z$$

$$= (18 + 20)x + (-18 + 36)z$$

$$\vec{D}_{7} = 38x + 18z/$$

(d) Calculate the magnitude and direction of \vec{D}_T .

$$|\vec{D}_{\tau}| = (38^{2} + 18^{2})^{1/2} = 42 \text{ km}$$

$$\Theta_{\tau} = \tan^{-1} \left(\frac{18}{38}\right) = 25^{\circ}$$

Vector Problems

After moving three times, you find yourself 5.39 m away from where you started and 21.8° below the x-axis. Your first move was 5.00 m at an angle of 53.1°. Your second move was 6.00 m along the x-axis and some unknown distance along the y-axis. Your third move was some unknown distance along the x-axis and -3.00 m along the y-axis.

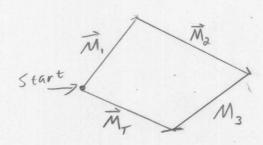


(a) Write each of the four vectors in unit vector notation.

 $\vec{M}_{F} = 5.39 \cos(51.8) \mathcal{X} + 5.39 \sin(-21.8) \mathcal{J}$ $\vec{M}_{F} = 52 - 2 \mathcal{J}$ $\vec{M}_{A} = 5.0 \cos(53.1) \mathcal{X} + 5.0 \sin(53.1) \mathcal{J}$ $\vec{M}_{A} = 3.0 \mathcal{X} + 4.0 \mathcal{J}$ $\vec{M}_{A} = 6.0 \mathcal{X} + 7.3 \mathcal{J}$ $\vec{M}_{B} = X_{B} - 3.0 \mathcal{J}$

(b) Calculate the unknown components of your second and third move. Make a sketch of the system.

 $\vec{M}_1 + \vec{M}_2 + \vec{M}_3 = \vec{M}_7$ $\chi: 3.0 \text{ m} + 6.0 \text{ m} + X_3 = 5 \text{ m} \implies X_3 = -4 \text{ m}$ $y: 4.0 \text{ m} + Y_2 - 3.0 \text{ m} = -2 \text{ m} \implies Y_3 = -3 \text{ m}$



Sample Test 1 Phys 111 Fall 2008

- 2) Consider 3 vectors. Vector **A** is given by $4.00i + A_yj$, vector **B** has a magnitude of 6.00 and is pointing at an angle of 35.0° with respect to the x axis, and vector **C** is given by $C_xi + 7.00j$.
- a. (10pts) Assuming that A + B = C, find the missing components A_y and C_x .
- b. (5pts) Find the magnitude of C?
- c. (5pts) Find the angle of C makes with respect to the x axis?

a)
$$A_x + B_x = + C_x$$

 $4.0 + 6 \cos 35 = + C_x$
 $C_x = 8.9$
 $A_y + B_y = C_y$
 $A_y + 6 \cot 35 = 7.0$
 $A_y = 3.56$
b) $||\dot{c}|| = (8.9^2 + 7.0^3)^{\frac{1}{2}} = 11.3$

Alice travels 2.00 km at $20^{\rm o}$ E of N to the first site and then 2.50 km at $11^{\rm o}$ N of E to the next.

Ben travels 3.00 km at 150 S of E to his first site.

- a) Write **analytical** expressions (no numbers) for the \mathbf{x} and \mathbf{y} components of the displacement required for Ben to meet Alice.
- b) Plug the numbers into your analytical equation and get a numeric answer.
- c) Convert the x and y components into magnitude and direction.

Make a clear sketch of the situation. In the sketch, define your coordinate system and all appropriate variables.

Vector equation
$$\overrightarrow{A}, + \overrightarrow{A}, = \overrightarrow{B}, + \overrightarrow{B},$$

$$\overrightarrow{B}, = \overrightarrow{A}, + \overrightarrow{A}, - \overrightarrow{B},$$

$$\overrightarrow{B}, = 2.0 \text{ km}, A_1 = 2.5 \text{ km}, B_1 = 3.0 \text{ km}$$

$$B_{2x} = A_{1x} + A_{2x} - B_{1x}$$

$$B_{2x} = A_{1} \leq A_{2x} + A_{3x} - B_{1x}$$

$$B_{3x} = A_{1} \leq A_{1} \leq A_{2x} + A_{3x} - B_{1x}$$

$$B_{3x} = A_{1} \leq A_{1} \leq A_{2x} + A_{3x} - B_{1x}$$

$$y: B_{3y} = A_{1y} + A_{3y} - B_{1y}$$

$$B_{3y} = A_{1}COS\Theta_{1} + A_{3}SIN\Theta_{2} - B_{1}SIN\Theta_{3}$$

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$$B_{2x} = 2.05IN(20) + 2.5COS(11) - 3.0COS(-15)$$

$$B_{3x} = 0.24 \text{ km}$$

$$B_{3y} = 2.0COS(20) + 2.55IN(11) - 3.05IN(-15)$$

$$B_{3y} = 3.1 \text{ km}$$

(c)
$$|\vec{B}_2| = (0.24^2 + 3.1^2)^{1/2}$$
 $\Theta_4 = \tan^{-1} \left(\frac{3.1}{0.24} \right)$ $|\vec{B}_2| = 3.1 \text{ km}$