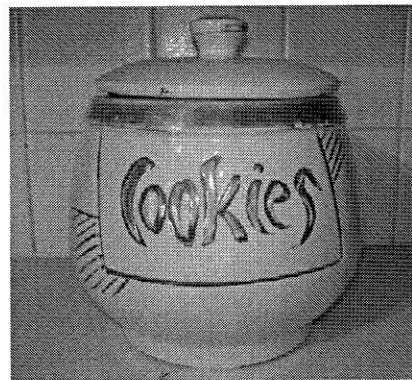


Force Problems – Set 1

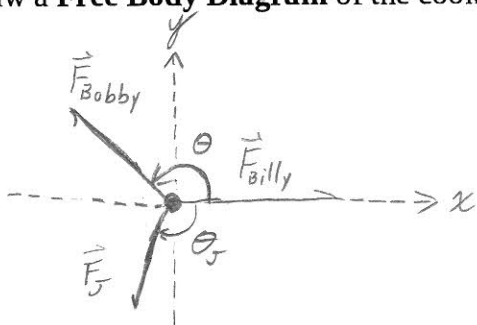
Bobby, Billy, and Jane are fighting over a cookie jar each pulling it in a different direction. As a result of their tussle, the jar's acceleration is zero. Bobby is pulling with a force of 10 N. Billy is pulling with a force of 12 N at an angle of 150° degrees with respect to the direction that Bobby is pulling.



a) What is the Net Force on the jar?

if $\vec{a} = 0$, then $\vec{F}_{net} = 0$

b) Draw a Free Body Diagram of the cookie jar. Include a coordinate system.



$$|\vec{F}_{Bobby}| = 10\text{ N}$$

$$|\vec{F}_{Billy}| = 12\text{ N}$$

$$\theta = 150^\circ$$

c) Write Newton's Second Law for each axis.

$$x: F_{Bobbyx} + F_{Billyx} + F_{Jx} = ma_x$$

$$y: F_{Bobbyy} + F_{Billyy} + F_{Jy} = ma_y$$

$$x: |\vec{F}_{Bobby}| \cos(\theta) + |\vec{F}_{Billy}| \cos\theta + F_{Jx} = 0$$

$$y: |\vec{F}_{Bobby}| \sin(\theta) + |\vec{F}_{Billy}| \sin\theta + F_{Jy} = 0$$

b) Solve the above system of equations for the components of Jane's force and find the magnitude and angle of her force with respect to Billy's.

$$F_{Jx} = -|\vec{F}_{Bobby}| \cos(\theta) - |\vec{F}_{Billy}| \cos\theta$$

$$F_{Jy} = -|\vec{F}_{Bobby}| \sin(\theta) - |\vec{F}_{Billy}| \sin\theta$$

$$F_{Jx} = -10 \cdot \cos(\theta) - 12 \cos(150)$$

$$F_{Jy} = 0 - 12 \cdot \sin(150)$$

$$F_{Jx} = 0.39\text{ N}$$

$$F_{Jy} = -6.0$$

$$|\vec{F}_{Jx}| = (0.39^2 + 6^2)^{1/2} = \boxed{6.01\text{ N}}$$

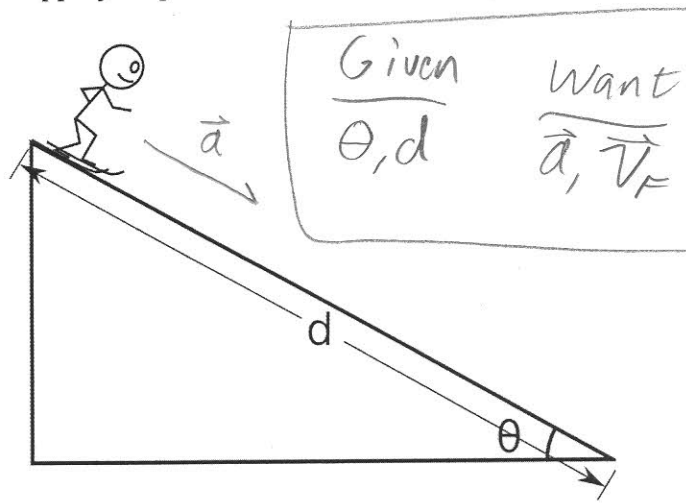
$$\theta_J = \tan^{-1}\left(\frac{-6.0}{0.39}\right)$$

$$\boxed{\theta_J = -86^\circ}$$

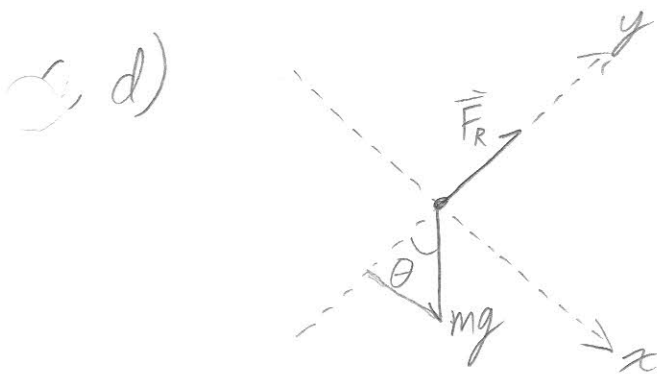
Force Problems – Set 1

A very talented stick skier is accelerating down a VERY slippery slope. (there's no friction, that's next period).

- List all of the forces on the skier.
- In what direction will the skier accelerate? Draw the acceleration vector in the picture at the right.
- Draw a *Free Body Diagram* for the skier.
- Choose a coordinate system and superimpose it on your free body diagram.
- Write the x and y versions of Newton's Second Law for the skier based on your coordinate system. Solve these equations for acceleration.
- What's the skier's velocity after accelerating a distance d?



a) Gravity, Reaction Force from slope



Rotate coordinate system to align x with the a vec.

e)

$$\sum F_x = ma_x$$

$$mg \sin \theta = ma_x$$

$$a_x = g \sin \theta$$

no accel in y

$$\sum F_y = ma_y$$

$$F_R - mg \cos \theta = 0$$

$$F_R = mg \cos \theta$$

$a_y = 0$

continued
↓

Force Problems - Set 1, P2 continued

(2)

g) Now use kinematics. But, only x since nothing is happening in y .

$$x = x_0 + v_{0x}t + \frac{1}{2}a_x t^2$$

$$v_x = v_0 + a_x t$$

$$d = \frac{1}{2}a_x t^2$$

$$v_x = a_x t \Rightarrow$$

$$t = \frac{v_x}{a}$$

$$d = \frac{1}{2}a_x \frac{v_x^2}{a_x^2} \Rightarrow d = \frac{v_x^2}{2a_x}$$

$$\Rightarrow v_x = (2da_x)^{1/2}$$

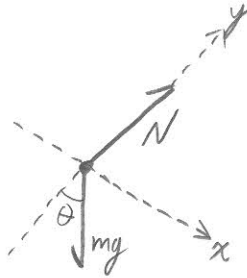
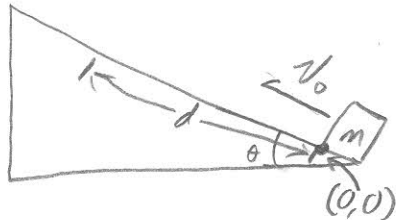
$$\Rightarrow v_x = (2dg \sin \theta)^{1/2}$$

Force Problems – Set 1

6

A block is given an initial velocity of 5 m/s up a frictionless 20° incline. How far up the incline does the block slide before coming to rest?

a) Draw a free body diagram of the block



Given
 $v_0 = 5 \text{ m/s}$
 $\theta = 20^\circ$
 $d = ? \leftarrow \text{want}$

b) Put a coordinate system on your free body diagram and, from the resulting picture, write Newton's second law for the x axis and for the y axis. Solve these equations for the acceleration of the block.

$$x: mg \sin \theta = ma_x \Rightarrow a_x = g \sin \theta$$

$$y: N - mg \cos \theta = 0$$

c) Use the kinematics equations and the acceleration from part b to find the distance.

$$x = x_0 + v_0 t + \frac{1}{2} a_x t^2$$

$$-d = 0 - v_0 t + \frac{1}{2} g \sin \theta t^2$$

$$-d = \frac{-v_0^2}{g \sin \theta} + \frac{1}{2} \frac{v_0^2}{g \sin \theta}$$

$$v = v_0 + a_x t$$

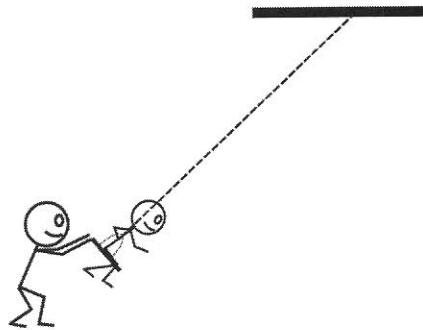
$$0 = -v_0 + g \sin \theta t$$

$$t = \frac{v_0}{g \sin \theta}$$

$$d = -\frac{v_0^2}{2g \sin \theta} = \frac{-5^2}{(2)(9.8) \sin(20)} = \boxed{-3.7 \text{ m}}$$

Force Problems – Set 1

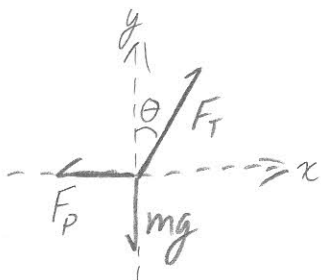
A 30-kg child is seated in a swing of negligible mass. Her father is pulling her back and is just about to let her go. How much **horizontal** force must her father apply so that the child and swing is held stationary the chain makes an angle of 32° with the vertical?



a) What is the child's acceleration?

$a = 0$, child is not moving

b) Draw a free body diagram of the system. Choose and label a coordinate system.



Given	Want
$m = 30 \text{ kg}$	$F_p = ?$
$\theta = 32^\circ$	
$a = 0$	

c) Using the picture from part b, write Newton's Second Law for the x-axis and the y-axis. Solve these equations for the required force.

$$\sum \vec{F} = m\vec{a} \Rightarrow \vec{F}_p + \vec{F}_T + m\vec{g} = m\vec{a}$$

$$x: F_T \sin \theta - F_p = 0 \Rightarrow F_T \sin \theta = F_p$$

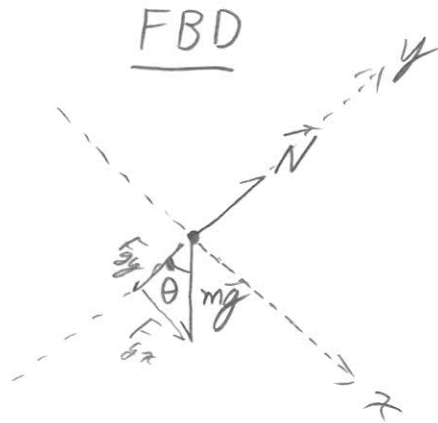
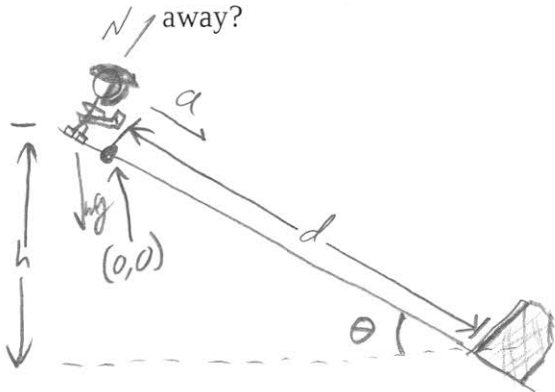
$$y: F_T \cos \theta - mg = 0 \Rightarrow F_T \cos \theta = mg$$

Divide x by y: $\frac{F_T \sin \theta}{F_T \cos \theta} = \frac{F_p}{mg} \Rightarrow \boxed{F_p = mg \tan \theta}$

$$F_p = (30)(9.8)(\tan 32) = \boxed{184 \text{ N}}$$

Force Problems – Set 1

A terrible earthquake has happened in San Francisco right in the middle of a critical hockey tournament. As a result of the quake, the ice rink is tilted 15° from horizontal. The 80 kg goalie begins to slide down the slope uncontrollably from his net directly into the opposing goalies net. How fast is he when he crosses the opposite goal line 53 m away?



Given
 $\theta = 15^\circ$
 $m = 80 \text{ kg}$
 $d = 53 \text{ m}$

$v_f = ? \leftarrow \text{want}$

Find the acceleration

$$\vec{F}_{\text{net}} = m\vec{a} \Rightarrow \text{NSL}$$

$$x: N_x + F_{gx} = ma_x$$

$$0 + mg \sin \theta = ma_x \Rightarrow \boxed{a_x = g \sin \theta}$$

$$y: N_y + F_{gy} = 0$$

$$N_y - mg \cos \theta = \underline{0} \Rightarrow \underline{N_y = mg \cos \theta}$$

no acceleration in the y

okay...
not useful here...

continued ↓

Ice rink continued

2

We have acceleration, now find v_f using kinematics.

But there's only action in x :

$$x = x_0 + v_{0x}t + \frac{1}{2}a_x t^2$$

$$v = v_0 + at$$

$$\textcircled{1} d = 0 + 0 + \frac{1}{2}g \sin \theta t^2$$

$$\textcircled{2} v_f = 0 + g \sin \theta t$$

acceleration is in positive x

Solve $\textcircled{1}$ for t and plug into $\textcircled{2}$

$$\text{From } \textcircled{1}: t = \left[\frac{2d}{g \sin \theta} \right]^{\frac{1}{2}}$$

$$\text{into } \textcircled{2}: v_f = g \sin \theta \left[\frac{2d}{g \sin \theta} \right]^{\frac{1}{2}}$$

$$v_f = (2gd \sin \theta)^{\frac{1}{2}}$$

hmm... $d \sin \theta = h$

$$v_f = [(2)(9.8)(53) \sin(15)]^{\frac{1}{2}} = 16.4 \text{ m/s}$$

Force Problems – Set 1

7

A 52 kg circus performer slides down a rope that will break if the tension exceeds 425 N.

- What happens if the performer hangs stationary from the rope?
- At what acceleration will the performer just avoid breaking the rope?



Given

$$F_{Tmax} = 425 \text{ N}$$

$$m = 52 \text{ kg}$$

Want

Part a: F_T

Part b: a_{min}

NSL: $\Sigma F = ma$

$$F_T - mg = ma$$

- Stationary performer, (or performer at constant v):

$$a = 0$$

$$\Rightarrow F_T - mg = 0 \Rightarrow \boxed{F_T = mg}$$

$$F_T = (52 \text{ kg})(9.8 \text{ m/s}^2) = \underline{510 \text{ N}}$$

Rope breaks.

- Accelerating performer: $F_T = ma + mg < F_{Tmax}$

$$\text{or: } \boxed{a < \frac{F_{Tmax}}{m} - g} \Rightarrow a < \frac{425 \text{ N}}{52 \text{ kg}} - 9.8 \text{ m/s}^2$$

$$a < \textcircled{-1.6 \text{ m/s}^2} \text{ or less.}$$